

# 20 years of semantic web data management

from an optimization point of view

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# Introduction

# The rise of semantic web data management (1/2)

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Till the end of the 20<sup>th</sup> century, there have been very few interaction between

- the **Database (DB)** community
  - data management w.r.t. simple mathematical structures for the sake of efficiency
- the **Knowledge Representation & Reasoning (KRR)** community
  - data management w.r.t. human cognitive schemes for the sake of intelligibility.

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At the beginning of the 21<sup>th</sup> century, a joint effort between DB and KRR led to the new era of **knowledge-based data management**.

It makes data management **one step closer to end-users** by advocating the use of:

- conceptual models from KRR as **human intelligible front-ends called ontologies**
- data models from DB as **efficient back-end storage**.

## The rise of semantic web data management (2/2)

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The **World Wide Web Consortium (W3C)** has strongly contributed to the success of knowledge-based data management with its **semantic web recommendations**, i.e., **standards for knowledge-based data management**:

- the Resource Description Framework (RDF) - a simple graph data model
- the Web Ontology Language (OWL2) - lightweight description logic data models
- the SPARQL query language - a SQL-like query language for RDF/OWL2.

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The advent of the RDF/OWL2/SPARQL standards has focused the attention on **practical semantic web data management**, which led to:

- key research contributions in Artificial Intelligence, Databases and Web venues
- key industrial or open source software (Jena, Oracle, RDFox, ...)

## The rise of semantic web data management (2/2)

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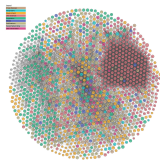
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**Large societies** have promptly adhered to semantic web data management!



# The semantic web data management challenge

---

**Knowledge-based/Semantic web data management** consists in  
**performing DB management tasks**

- e.g., consistency checking, query answering, etc.

**on knowledge bases (KBs) expressed in (or inspired from) KRR languages**

- e.g., RDF, description logics/OWL2, datalog $\pm$ /existential rules, etc.

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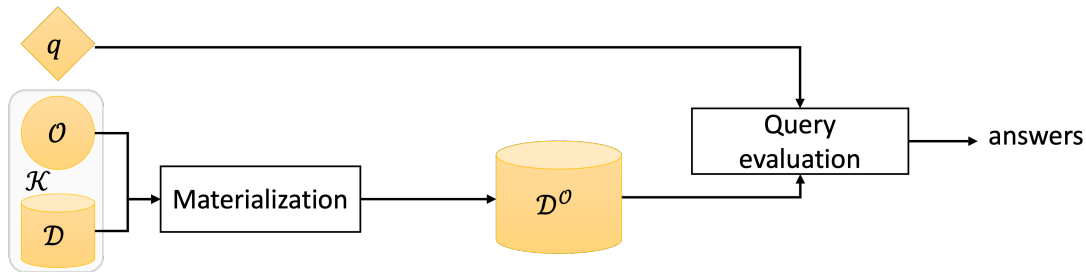
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Performing these tasks correctly requires automated reasoning, **which comes at a price!**

We focus on ontology-mediated query answering (OMQA), i.e., query answering on KBs

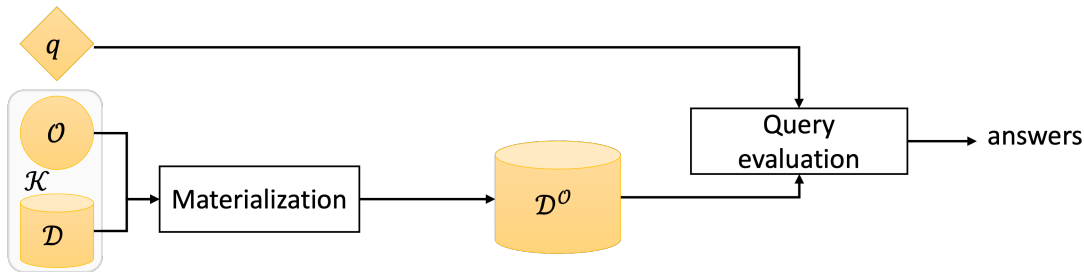
# OMQA via materialization (not the topic of this talk)

**Materialization** compiles domain knowledge into the data.



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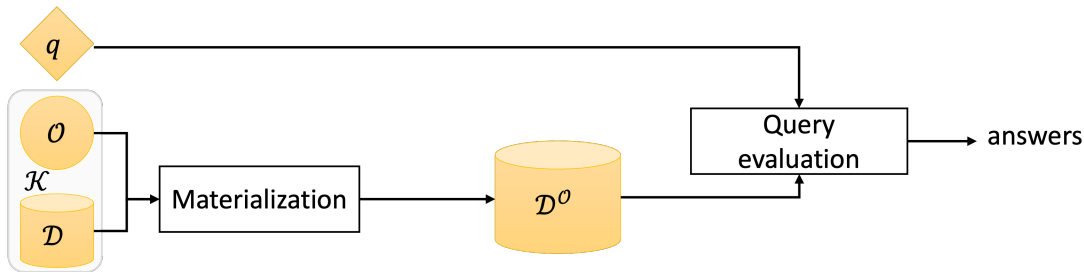
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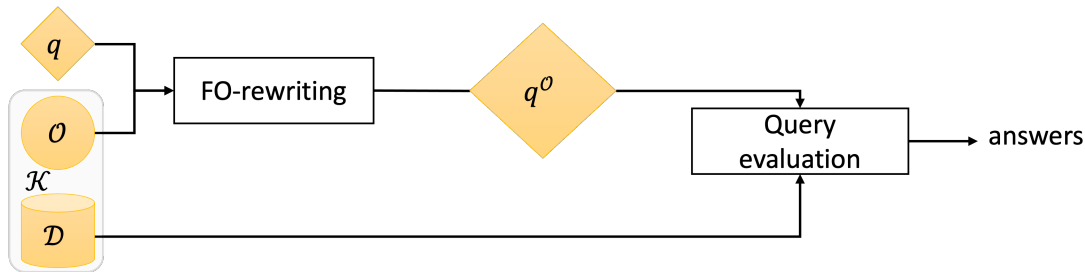
When it is possible, it

- + is **fast at query time**

- needs **efficient maintenance** when the database is updated  $\Rightarrow$  **optimization!**

# OMQA via FO-rewriting (topic of this talk)

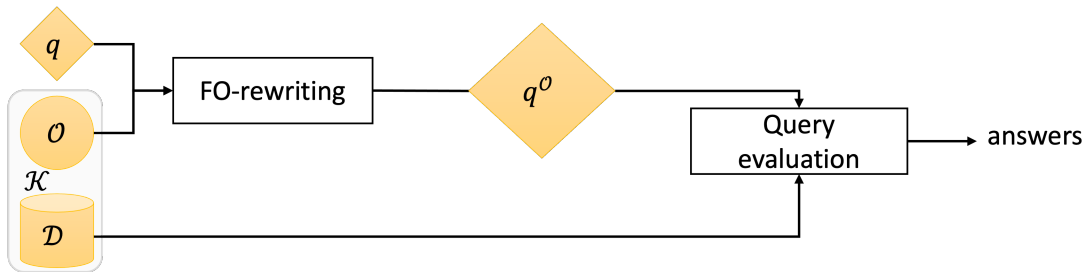
**FO-rewriting** compiles domain knowledge into the queries.



**FO-rewriting is not always possible!**

# OMQA via FO-rewriting (topic of this talk)

**FO-rewriting** compiles domain knowledge into the queries.



**FO-rewriting is not always possible!**

When it is possible, it

- + does not need **maintenance** when the database is updated.
- may produce complex rewritings that are **challenging to evaluate**  $\Rightarrow$  **optimization!**

# Overview

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1. Introduction
2. Preliminaries
3. Act I: OMQA via FO-rewriting
4. Act II: query rewriting languages
5. Act III: data-dependent optimization of rewritings
6. Conclusion and perspectives

# Preliminaries

# Queries

We consider FO queries of the form  $q(\bar{x}) = \phi$  with  $\bar{x}$  the free variables of the formula  $\phi$ .

We will start with the following query languages:

| Language | First-Order Logic syntax                                  | Relational algebra syntax                            |
|----------|-----------------------------------------------------------|------------------------------------------------------|
| CQ       | $q(\bar{x}) = (\exists \bar{y}) \bigwedge_{i=1}^n atom_i$ | $q(\bar{x}) = \Pi_{\bar{x}}(\bowtie_{i=1}^n atom_i)$ |
| UCQ      | $q(\bar{x}) = \bigvee_{i=1}^n CQ_i$                       | $q(\bar{x}) = \bigcup_{i=1}^n CQ_i$                  |

## Running example

We consider the CQ asking for the supervisees who work with **h** that is a researcher:

$$q(x) = (\exists y) R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge sup(y, x).$$

## Knowledge bases (KBs)

We consider FO KBs expressed using **existential rules**.

A **KB**  $\mathcal{K} = (\mathcal{O}, \mathcal{D})$  such that

- $\mathcal{O}$  is an **ontology** made of rules of the form  $\forall \bar{x} (body(\bar{x}) \rightarrow head(\bar{x}))$ , where  $body(\bar{x})$  and  $head(\bar{x})$  are CQs, denoted w.l.o.g. by  $body(\bar{x}) \rightarrow head(\bar{x})$
- $\mathcal{D}$  is a **database** is a set of incomplete facts.

The semantics of  $\mathcal{K}$  is that of the formula:  $\bigwedge_{r \in \mathcal{O}} r \wedge \exists \bar{v} \bigwedge_{f \in \mathcal{D}} f$  with  $\bar{v}$  the variables in  $\mathcal{D}$ .

### Running example (cont.)

We consider the KB  $\mathcal{K} = (\mathcal{O}, \mathcal{D})$  such that:

$$\mathcal{O} = \{r_1 = ww(x, y) \rightarrow ww(y, x), r_2 = sup(x, y) \rightarrow ww(x, y), r_3 = PhD(x) \rightarrow sup(y, x)\}$$

and

$$\mathcal{D} = \{R(\mathbf{f}), R(\mathbf{h}), sup(\mathbf{f}, \mathbf{w}), sup(\mathbf{h}, \mathbf{w}), PhD(\mathbf{w}), ww(\mathbf{f}, \mathbf{h}), R(u), ww(u, \mathbf{c}), PhD(\mathbf{c})\}$$

# Ontology-mediated query answering (OMQA)

We consider the standard **certain answer semantics** for OMQA.

A **(certain) answer to a query**  $q(\bar{x})$  of arity  $n$  on a KB  $\mathcal{K}$  is a tuple  $\bar{\mathbf{t}}$  of  $n$  constants from  $\mathcal{K}$  such that  $\mathcal{K} \models q(\bar{\mathbf{t}})$ , where

- $\models$  is the FO entailment relation
- $q(\bar{\mathbf{t}})$  is the Boolean query obtained by instantiating  $\bar{x}$  with  $\bar{\mathbf{t}}$  in  $q$ .

We denote by  $ans(q, \mathcal{K})$  the *answer set* of  $q$  on  $\mathcal{K}$ .

## Running example (cont.)

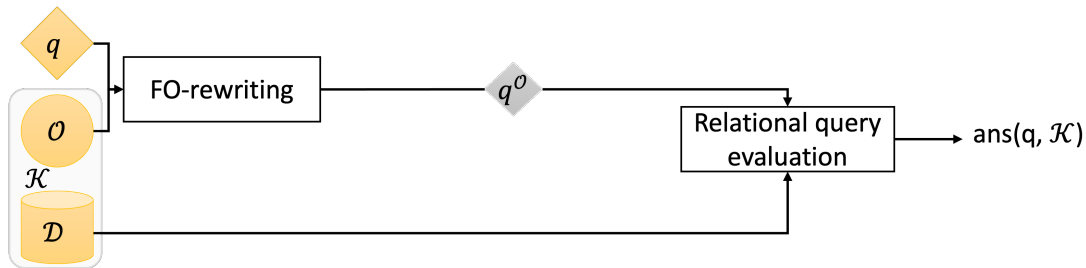
The answer set of  $q(x) = R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge sup(y, x)$  on  $\mathcal{K}$  is  $ans(q, \mathcal{K}) = \{\langle \mathbf{w} \rangle\}$ :

- $R(\mathbf{h}) \in \mathcal{D}$
- the fact  $ww(\mathbf{h}, \mathbf{w})$  entailed from  $sup(\mathbf{h}, \mathbf{w}) \in \mathcal{D}$  and  $r_2 = sup(x, y) \rightarrow ww(x, y)$
- either  $sup(\mathbf{f}, \mathbf{w}) \in \mathcal{D}$  or  $sup(\mathbf{h}, \mathbf{w}) \in \mathcal{D}$ .

# Act I: OMQA via FO-rewriting

# OMQA via FO-rewriting

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# OMQA via FO-rewriting by example

## Running example (cont.)

The query rewriting of

$$q(x) = R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge sup(y, x)$$

w.r.t.

$$\mathcal{O} = \{r_1 = ww(x, y) \rightarrow ww(y, x), r_2 = sup(x, y) \rightarrow ww(x, y), r_3 = PhD(x) \rightarrow sup(y, x)\}$$

is:

$$\begin{aligned} q_{UCQ}^{\mathcal{O}}(x) &= (R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge sup(y, x)) \quad (1) \\ &\vee (R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge PhD(x)) \quad (2) = (1) + r_3 \\ &\vee (R(\mathbf{h}) \wedge sup(\mathbf{h}, x) \wedge \cancel{sup(y, x)}) \quad (3) = (1) + r_2 \\ &\vee (R(\mathbf{h}) \wedge ww(x, \mathbf{h}) \wedge sup(y, x)) \quad (4) = (1) + r_1 \\ &\vee (R(\mathbf{h}) \wedge ww(x, \mathbf{h}) \wedge PhD(x)) \quad (5) = (2) + r_1 \text{ or } (4) + r_3 \\ &\vee (R(\mathbf{h}) \wedge sup(x, \mathbf{h}) \wedge sup(y, x)) \quad (6) = (4) + r_2 \\ &\vee (R(\mathbf{h}) \wedge sup(x, \mathbf{h}) \wedge PhD(x)) \quad (7) = (5) + r_2 \text{ or } (6) + r_3 \end{aligned}$$

# OMQA via FO-rewriting by example

## Running example (cont.)

The answer set of  $q$  w.r.t.  $\mathcal{K} = (\mathcal{O}, \mathcal{D})$  is then obtained by the relational evaluation of

$$q_{\text{UCQ}}^{\mathcal{O}}(x) = (R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge sup(y, x)) \quad (1)$$

$$\vee (R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge PhD(x)) \quad (2)$$

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$$\mathcal{D} = \{R(\mathbf{f}), R(\mathbf{h}), sup(\mathbf{f}, \mathbf{w}), sup(\mathbf{h}, \mathbf{w}), PhD(\mathbf{w}), ww(\mathbf{f}, \mathbf{h}), R(u), ww(u, \mathbf{c}), PhD(\mathbf{c})\}$$

$$\text{i.e., } ans(q, \mathcal{K}) = eval(q_{\text{UCQ}}^{\mathcal{O}}, \mathcal{D}) = \{\langle \mathbf{w} \rangle\}.$$

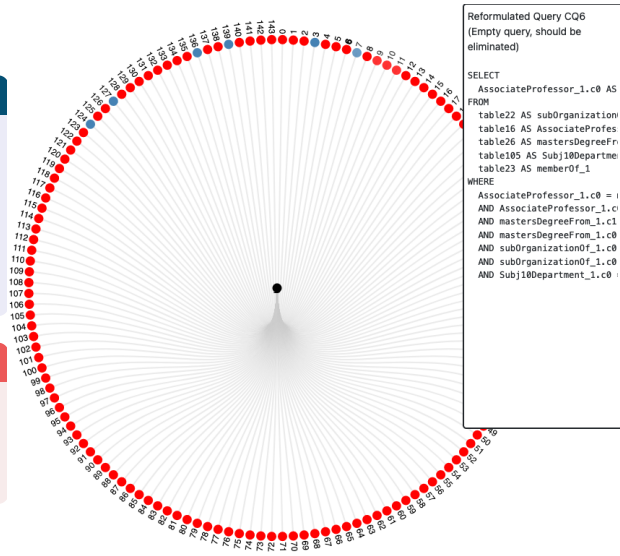
# OMQA via FO-rewriting is computationally expensive

## Cost of FO-rewriting

- The worst-case size of a rewriting  $q^{\circ}$  is **exponential** in the size of  $q$  even for lightweight ontology languages
- The time to compute  $q^{\circ}$  is **negligible** w.r.t. the time of its evaluation on  $\mathcal{D}$ .

## Cost of evaluating a query rewriting

Query rewritings may be **complex** in practice and **challenging to evaluate**, even for highly-optimized RDBMSs.



## Take home message

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1. FO-rewriting **reduces** query answering on KBs to query answering on databases
2. FO-rewriting is **computationally expensive**
3. FO-rewriting needs to be **optimized for RDBMSs**

## Related work and contributions

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Some references from the literature on devising OMQA via FO-rewriting for CQs:

|                                  | <b>Query rewriting language</b>            |
|----------------------------------|--------------------------------------------|
| <b>Ontology language</b>         | UCQ                                        |
| datalog $\pm$ /existential rules | [GOP11, GOP14, KLMT15]                     |
| description logics/OWL           | [CDL <sup>+</sup> 07, PHM09, CTS11, VSS12] |
| RDFS                             | <b>[GMR13, BGMM19]</b>                     |

## **Act II: query rewriting languages**

# FO-rewriting optimization: two main options

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## 1. Produce query rewritings faster

- conceptually interesting but of limited interest from the practical point of view
  - time to produce the rewriting  $\ll$  time to evaluate the rewriting on the database

## 2. Make the query rewritings faster to evaluate

## Key observation: UCQ rewritings are highly redundant!

Logical redundancy in rewritings = redundant computation when rewritings are evaluated!

### Running example (cont.)

The query rewriting of  $q(x) = R(\mathbf{h}) \wedge ww(\mathbf{h}, x) \wedge sup(y, x)$  w.r.t.

$$\mathcal{O} = \{r_1 = ww(x, y) \rightarrow ww(y, x), r_2 = sup(x, y) \rightarrow ww(x, y), r_3 = PhD(x) \rightarrow sup(y, x)\}$$

is:

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# Taming redundancy in rewritings: minimal UCQ rewritings

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FO-rewriting techniques have been proposed to compute UCQ rewritings within which:

- each CQ is minimal (no redundant subCQs)
- no CQ is redundant with another

## Pros & cons of such techniques

- + Such techniques optimize UCQ rewritings to the possible extent
- Limited performance improvement
  - The size of a **minimal** UCQ rewriting is **exponential** in the size of the query even for lightweight ontology languages
  - **Minimal** UCQ rewritings are **highly redundant**

# Minimal UCQ rewritings are highly redundant!

## Running example (cont.)

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# Taming redundancy in rewritings: compact USCQ rewritings

---

**Breakthrough in 2013:** adopting a (relational) rewriting language other than UCQ!

[Tho13] introduces an FO-rewriting technique with USCQ as a rewriting language for **compact rewritings that drastically limit redundancy**.

| Language | First-Order Logic syntax                                                        | Relational algebra syntax                                                  |
|----------|---------------------------------------------------------------------------------|----------------------------------------------------------------------------|
| SCQ      | $q(\bar{x}) = (\exists \bar{y}) \bigwedge_{i=1}^n \bigvee_{j=1}^{m_i} atom_i^j$ | $q(\bar{x}) = \Pi_{\bar{x}}(\bowtie_{i=1}^n \bigcup_{j=1}^{m_i} atom_i^j)$ |
| USCQ     | $q(\bar{x}) = \bigvee_{i=1}^n SCQ_i$                                            | $q(\bar{x}) = \bigcup_{i=1}^n SCQ_i$                                       |

# Taming redundancy in rewritings: compact USCQ rewritings

This allows a shift from highly redundant rewritings. . .

## Running example (cont.)

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# Taming redundancy in rewritings: compact USCQ rewritings

... to rewriting with limited redundancy.

## Running example (cont.)

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$$\begin{aligned} q_{\text{USCQ}}^{\mathcal{O}}(x) = & ( R(\mathbf{h}) ) \\ & \wedge ( ww(\mathbf{h}, x) \vee sup(\mathbf{h}, x) \vee ww(x, \mathbf{h}) \vee sup(x, \mathbf{h}) ) \\ & \wedge ( sup(y, x) \vee PhD(x) ) \end{aligned}$$

But... is this the killer rewriting language w.r.t. performance?

## Use case: asking CQs on RDF KBs

### Performance with different but equivalent query rewritings

---

Given the query

$q(x, y) = t(x, \text{rdf:type}, y),$  (a<sub>1</sub>)

$\wedge t(x, \text{lubm:degreeFrom}, \text{"http : //www.University532.edu"}),$  (a<sub>2</sub>)

$\wedge t(x, \text{lubm:memberOf}, \text{"http : //www.Department1.University7.edu"})$  (a<sub>3</sub>)

the LUBM100M dataset and a CQ-to-UCQ rewriting algorithm *rewrite*

| Rewriting                                                     | a.k.a. | PostgreSQL exec. time (ms) |
|---------------------------------------------------------------|--------|----------------------------|
| <i>rewrite(a<sub>1</sub> ∧ a<sub>2</sub> ∧ a<sub>3</sub>)</i> |        |                            |

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| Rewriting                                   | a.k.a. | PostgreSQL exec. time (ms) |
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| $\text{rewrite}(a_1 \wedge a_2 \wedge a_3)$ | UCQ    |                            |

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| $\text{rewrite}(a_1 \wedge a_2 \wedge a_3)$ | UCQ    | <b>6,387</b>               |

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| Rewriting                                                                   | a.k.a. | PostgreSQL exec. time (ms) |
|-----------------------------------------------------------------------------|--------|----------------------------|
| $\text{rewrite}(a_1 \wedge a_2 \wedge a_3)$                                 | UCQ    | <b>6,387</b>               |
| $\text{rewrite}(a_1) \wedge \text{rewrite}(a_2) \wedge \text{rewrite}(a_3)$ |        |                            |

## Use case: asking CQs on RDF KBs

### Performance with different but equivalent query rewritings

---

Given the query

$$q(x, y) = t(x, \text{rdf:type}, y), \quad (\mathbf{a_1})$$

$$\wedge t(x, \text{lubm:degreeFrom}, \text{"http : //www.University532.edu"}), \quad (\mathbf{a_2})$$

$$\wedge t(x, \text{lubm:memberOf}, \text{"http : //www.Department1.University7.edu"}) \quad (\mathbf{a_3})$$

the LUBM100M dataset and a CQ-to-UCQ rewriting algorithm *rewrite*

| Rewriting                                                                   | a.k.a. | PostgreSQL exec. time (ms) |
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| Rewriting                                                                   | a.k.a. | PostgreSQL exec. time (ms) |
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$\wedge t(x, \text{lubm:degreeFrom}, \text{"http : //www.University532.edu"}),$  (a<sub>2</sub>)

$\wedge t(x, \text{lubm:memberOf}, \text{"http : //www.Department1.University7.edu"})$  (a<sub>3</sub>)

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| Rewriting                                                                   | a.k.a. | PostgreSQL exec. time (ms) |
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| $\text{rewrite}(a_1 \wedge a_2 \wedge a_3)$                                 | UCQ    | <b>6,387</b>               |
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| $\text{rewrite}(a_1 \wedge a_2) \wedge \text{rewrite}(a_3)$                 |        | 1,968                      |
| $\text{rewrite}(a_1) \wedge \text{rewrite}(a_2 \wedge a_3)$                 |        | 846,710                    |
| $\text{rewrite}(a_1 \wedge a_3) \wedge \text{rewrite}(a_2)$                 |        | <b>554</b>                 |
| $\text{rewrite}(a_1 \wedge a_2) \wedge \text{rewrite}(a_1 \wedge a_3)$      |        | 2,734                      |
| $\text{rewrite}(a_1 \wedge a_2) \wedge \text{rewrite}(a_2 \wedge a_3)$      |        | 2,289                      |
| $\text{rewrite}(a_1 \wedge a_3) \wedge \text{rewrite}(a_2 \wedge a_3)$      |        | 588                        |

# Cost-based FO-rewriting

---

**Breakthrough in 2015-16:** 1 CQ  $\rightarrow$  N rewritings + cost model of rewriting evaluation

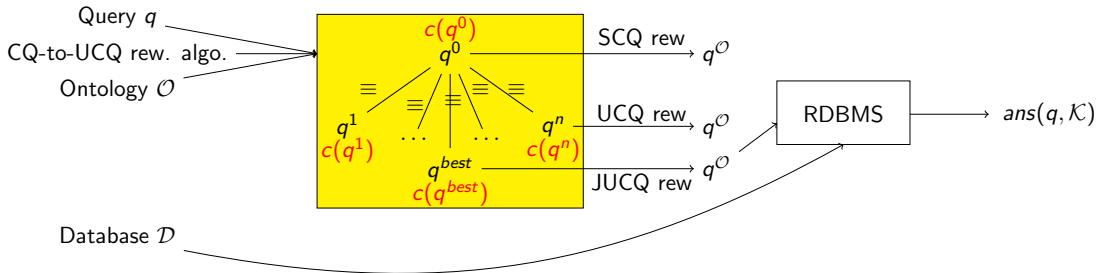
[BGM15, BGM16] introduces an FO-rewriting technique with JUCQ as a rewriting language so that:

- a CQ has a set of syntactically different but semantically equivalent rewritings
- out of which a rewriting with best estimated evaluation cost is selected.

| Language | First-Order Logic syntax                                  | Relational algebra syntax                            |
|----------|-----------------------------------------------------------|------------------------------------------------------|
| CQ       | $q(\bar{x}) = (\exists \bar{y}) \bigwedge_{i=1}^n atom_i$ | $q(\bar{x}) = \Pi_{\bar{x}}(\bowtie_{i=1}^n atom_i)$ |
| UCQ      | $q(\bar{x}) = \bigvee_{i=1}^n CQ_i$                       | $q(\bar{x}) = \bigcup_{i=1}^n CQ_i$                  |
| JUCQ     | $q(\bar{x}) = \bigwedge_{i=1}^n UCQ_i$                    | $q(\bar{x}) = \Pi_{\bar{x}}(\bowtie_{i=1}^n UCQ_i)$  |

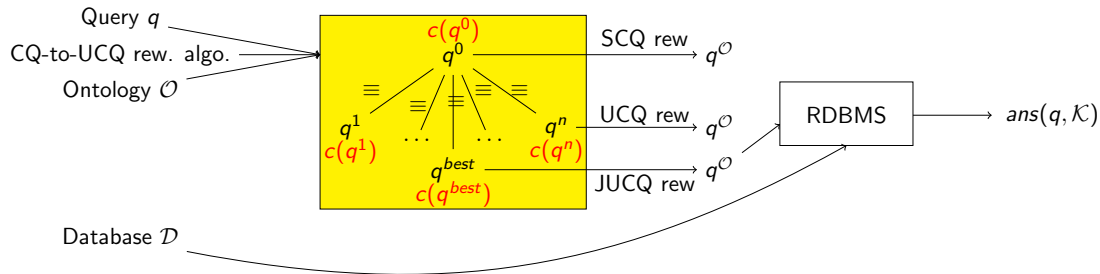
# Cost-based FO-rewriting: overview

To answer the CQ  $q$  on the KB  $\mathcal{K} = (\mathcal{O}, \mathcal{D})$ :



# Cost-based FO-rewriting: overview

To answer the CQ  $q$  on the KB  $\mathcal{K} = (\mathcal{O}, \mathcal{D})$ :



In general, the search space is too large for fast optimization time!

## Cost-based FO-rewriting: greedy CQ-to-JUCQ rewriting

---

Given the query

$$\begin{aligned} q(x, y) = & t(x, \text{rdf:type}, y), & (\mathbf{a_1}) \\ & \wedge t(x, \text{lubm:degreeFrom}, \text{"http : //www.University532.edu"}), & (\mathbf{a_2}) \\ & \wedge t(x, \text{lubm:memberOf}, \text{"http : //www.Department1.University7.edu"}) & (\mathbf{a_3}) \end{aligned}$$

a cost-based greedy exploration is:

$$\text{rewrite}(a_1) \wedge \text{rewrite}(a_2) \wedge \text{rewrite}(a_3)$$

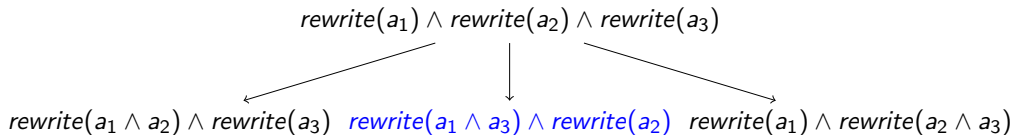
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## Cost-based FO-rewriting: greedy CQ-to-JUCQ rewriting

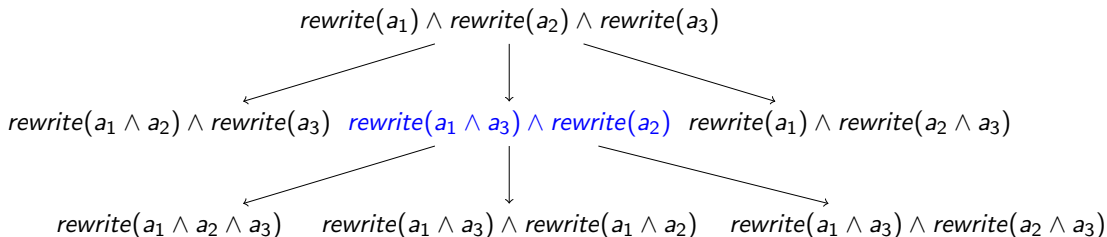
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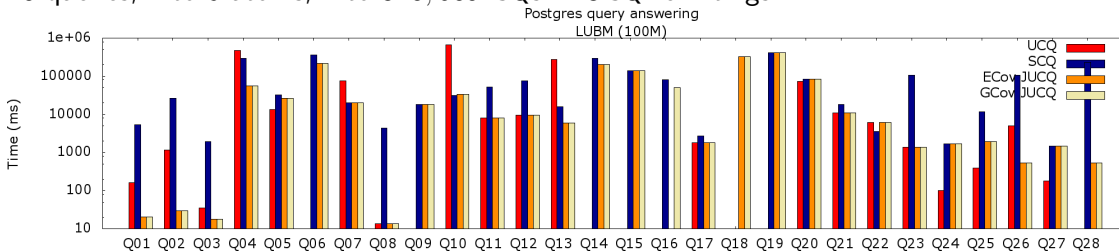
a cost-based greedy exploration is:



# Cost-based FO-rewriting: sample experimental results

## Query answering on LUBM 100 M using PostgreSQL

28 queries; 2 to 6 atoms; 1 to 318,089 CQs in UCQ rewritings



## Take home message

---

1. Alternative query rewritings may have **very different evaluation times**
2. A cost model for rewriting evaluation gives rapidly **estimations of evaluation costs**
3. Selecting a rewriting from alternative ones using a cost-model is **the best option**

## Related work and contributions

---

Some references from the literature on devising OMQA via FO-rewriting for CQs:

| Ontology language                | Query rewriting language                   |         |         |                       |
|----------------------------------|--------------------------------------------|---------|---------|-----------------------|
|                                  | UCQ                                        | USCQ    | JUCQ    | datalog <sup>nr</sup> |
| datalog $\pm$ /existential rules | [GOP11, GOP14, KLMT15]                     | [Tho13] |         | [OP11, GS12]          |
| description logics/OWL           | [CDL <sup>+</sup> 07, PHM09, CTS11, VSS12] |         | [BGM16] | [RA10]                |
| RDFS                             | [GMR13, BGMM19]                            |         | [BGM15] |                       |

## **Act III: data-dependent optimization of rewritings**

## Key observation: rewritings are too complex w.r.t. OMQA!

---

Complex rewritings = rewritings that are costly to evaluate by RDBMSs!

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Complex rewritings = rewritings that are costly to evaluate by RDBMSs!

### First-Order rewritability

Given a query language  $\mathcal{L}_Q$  and an ontology language  $\mathcal{L}_O$ , the OMQA setting  $(\mathcal{L}_Q, \mathcal{L}_O)$  is FO-rewritable iff for each  $q \in \mathcal{L}_Q$  and  $\mathcal{O} \in \mathcal{L}_O$  there exists an FO-query  $q^{\mathcal{O}}$  such that:

for each database  $\mathcal{D}$ ,  $ans(q, \langle \mathcal{O}, \mathcal{D} \rangle) = eval(q^{\mathcal{O}}, \mathcal{D})$

where  $eval(\cdot, \cdot)$  is the standard relational query evaluation.

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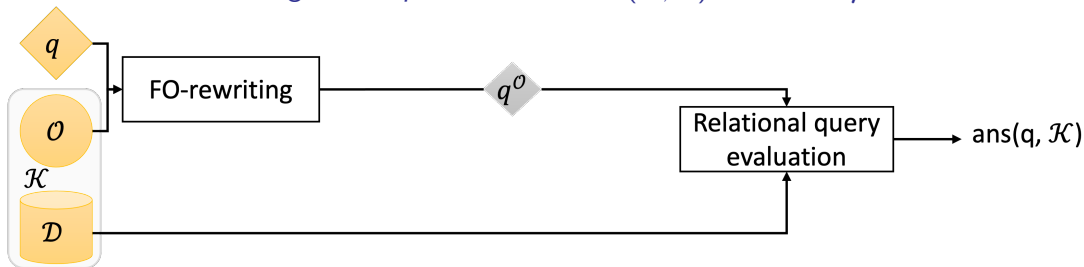
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where  $eval(\cdot, \cdot)$  is the standard relational query evaluation.

OMQA via FO-rewriting: when  $q$  is asked on  $\mathcal{K} = (\mathcal{O}, \mathcal{D})$ ,  $\mathcal{D}$  is **fixed/known!**



## Key observation: rewritings are too complex w.r.t. OMQA!

---

### A minimal UCQ rewriting models

- all the (worst-case exponentially many) non-redundant specializations of the query

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---

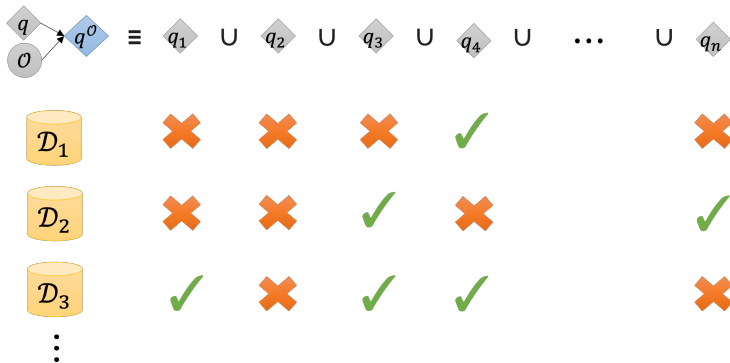
## A minimal UCQ rewriting models

- all the (worst-case exponentially many) non-redundant specializations of the query
- all the ways all the possible databases may store answers to the query!

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## A minimal UCQ rewriting models

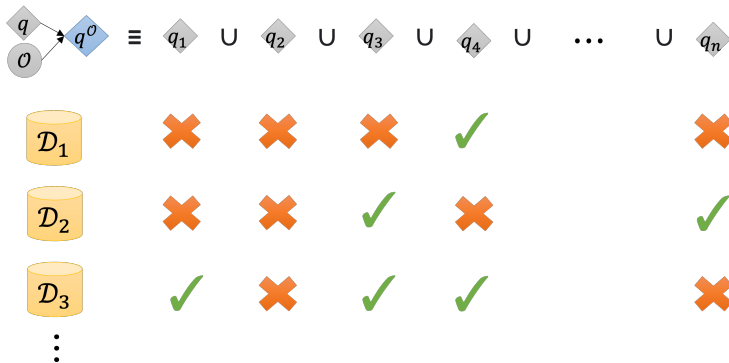
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## A minimal UCQ rewriting models

- all the (worst-case exponentially many) non-redundant specializations of the query
- all the ways all the possible databases may store answers to the query!



Any (USCQ, JUCQ, ...) rewriting is equivalent to a minimal UCQ rewriting, hence somehow models all the ways all the possible databases may store answers to the query!

# Key observation: rewritings are too complex w.r.t. OMQA!

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Breakthrough in 2021: data-dependent optimization of rewritings!

## Key observation: rewritings are too complex w.r.t. OMQA!

---

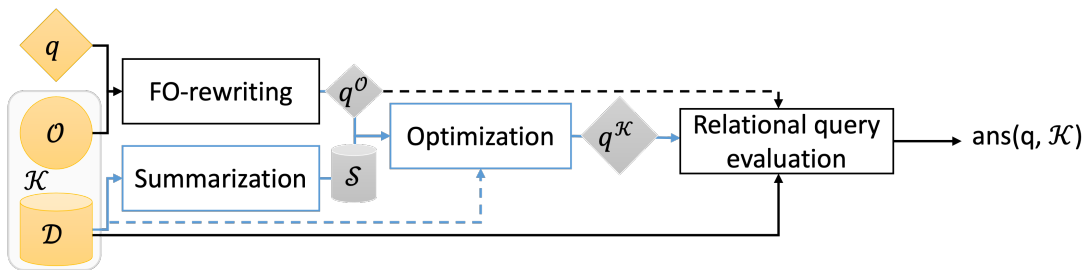
**Breakthrough in 2021:** data-dependent optimization of rewritings!

[HVGJ21, HVGJ23, HVGJ24] compute **simpler rewritings with the same answers (just) on the database at hand.**

# Key observation: rewritings are too complex w.r.t. OMQA!

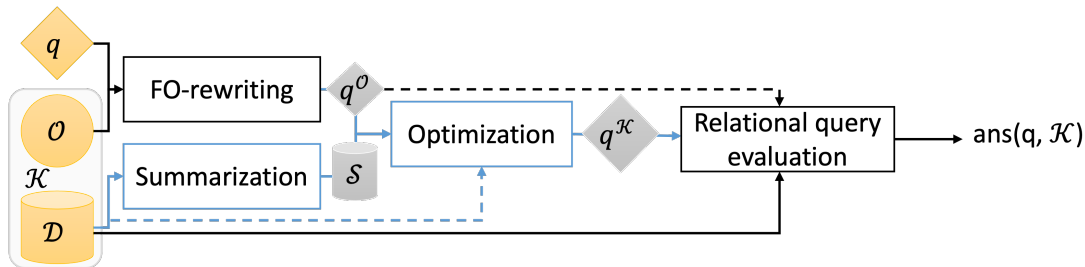
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# Data-dependent FO-rewriting: requirements

1. For **generality**, we optimize a  $(\wedge, \vee)$ -CQ rewriting  $q^{\mathcal{O}}$ 
  - Rewriting languages uses CQ as basic building block: **UCQ**, **USCQ** and **JUCQ**
2. For **correctness**, we use an optimization function  $\Omega$  such that  $q^{\mathcal{K}} = \Omega(q^{\mathcal{O}}, \mathcal{S})$  where
  - $q^{\mathcal{K}} \models q^{\mathcal{O}}$  for **soundness**
  - $eval(q^{\mathcal{O}}, \mathcal{D}) = eval(q^{\mathcal{K}}, \mathcal{D})$  for **completeness**
3. For **efficiency**, we require for a “relevant” cost function  $c$ :
  - $c(\Omega(q^{\mathcal{O}}, \mathcal{S})) + c(eval(q^{\mathcal{K}}, \mathcal{D})) \leq c(eval(q^{\mathcal{O}}, \mathcal{D}))$



# Data-dependent FO-rewriting: overview

---

**Optimization technique:** we rewrite a  $(\wedge, \vee)$ -CQ rewriting from the bottom up, **while propagating the effect of removing subCQs with no answers on the database.**

## (General) Database summary

A summary  $\mathcal{S}$  of a database  $\mathcal{D}$  is a **homomorphic approximation** of it:  $\mathcal{S} = \mathcal{D}_\sigma$  with  $\sigma$  a database-to-summary homomorphism that maps each variable in  $\mathcal{D}$  to a variable or constant in  $\mathcal{S}$ , and each constant in  $\mathcal{D}$  to constant in  $\mathcal{S}$ .

A database is a summary of itself, with  $\sigma$  the identity function.

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A database is a summary of itself, with  $\sigma$  the identity function.

## Identifying empty CQs with a database summary

If a CQ  $q$  has an answer on the database  $\mathcal{D}$ , then  $q_\sigma$  has an answer on its summary  $\mathcal{S}$

$\Leftrightarrow$

**If  $q_\sigma$  has no answer on  $\mathcal{S}$ , then  $q$  has no answer on  $\mathcal{D}$**

with  $\sigma$  the  $\mathcal{D}$ -to- $\mathcal{S}$  homomorphism.

# Data-dependent FO-rewriting: overview

In an optimization setting, summaries must be **small and fast to compute/maintain**.

(Concrete) Database summary: quotient database w.r.t. the  $\equiv_{\Omega}$  equivalence relation

- The database-to-summary homomorphism  $\sigma$  is defined by an equivalence relation on the database terms.
- We use the  $\equiv_{\Omega}$  equivalence relation such that  $t_1 \equiv_{\Omega} t_2$  iff:
  - $t_1, t_2$  are instances of a same unary relation/class/concept
  - $t_1 \equiv_{\Omega} t_3$  and  $t_2 \equiv_{\Omega} t_3$ .

Quotient databases can be rapidly computed/maintained via union-find-delete structures.

Running example (cont.)

$\mathcal{D} = \{R(\mathbf{f}), R(\mathbf{h}), \text{sup}(\mathbf{f}, \mathbf{w}), \text{sup}(\mathbf{h}, \mathbf{w}), \text{PhD}(\mathbf{w}), \text{ww}(\mathbf{f}, \mathbf{h}), R(u), \text{ww}(u, \mathbf{c}), \text{PhD}(\mathbf{c})\}$   
is summarized into

$$\mathcal{S} = \{R(\mathbf{r}), \text{sup}(\mathbf{r}, \mathbf{p}), \text{PhD}(\mathbf{p}), \text{ww}(\mathbf{r}, \mathbf{r}), \text{ww}(\mathbf{r}, \mathbf{p})\}$$

where  $\mathbf{r}$  represents  $\{\mathbf{f}, \mathbf{h}, u\}$  and  $\mathbf{p}$  represents  $\{\mathbf{w}, \mathbf{c}\}$ .

# Data-dependent FO-rewriting: overview

**Optimization technique:** we rewrite a  $(\wedge, \vee)$ -CQ rewriting from the bottom up, **while propagating the effect of removing subCQs with no answers on the database.**

## The $\Omega$ optimization function

- The optimization of a CQ  $q$  is:

$$\Omega(q, \mathcal{S}) = \begin{cases} \emptyset & \text{if } eval(q_\sigma, \mathcal{S}) = \emptyset \\ q & \text{otherwise} \end{cases} \quad (1)$$

where  $q_\sigma$  is obtained from  $q$  by replacing its constants by their images through  $\sigma$ .

- The optimization of a conjunction of subqueries  $\bigwedge_{i=1}^n q_i$  is:

$$\Omega\left(\bigwedge_{i=1}^n q_i, \mathcal{S}\right) = \begin{cases} \emptyset & \text{if } \exists i \in [1, n] \ \Omega(q_i, \mathcal{S}) = \emptyset \\ \bigwedge_{i=1}^n \Omega(q_i, \mathcal{S}) & \text{otherwise} \end{cases} \quad (2)$$

- The optimization of a disjunction of subqueries  $\bigvee_{i=1}^n q_i$  is:

$$\Omega\left(\bigvee_{i=1}^n q_i, \mathcal{S}\right) = \begin{cases} \emptyset & \text{if } \forall i \in [1, n] \ \Omega(q_i, \mathcal{S}) = \emptyset \\ \bigvee_{1 \leq i \leq n, \ \Omega(q_i, \mathcal{S}) \neq \emptyset} \Omega(q_i, \mathcal{S}) & \text{otherwise} \end{cases} \quad (3)$$

# Data-dependent FO-rewriting by example

## Running example (cont.)

The optimization of  $q_{\text{UCQ}}^{\mathcal{O}}$  with

$$\mathcal{S} = \{R(\mathbf{r}), \text{sup}(\mathbf{r}, \mathbf{p}), \text{PhD}(\mathbf{p}), \text{ww}(\mathbf{r}, \mathbf{r}), \text{ww}(\mathbf{r}, \mathbf{p})\}$$

and the database-to-summary homomorphism

$$\sigma(\mathbf{f}) = \sigma(\mathbf{h}) = \sigma(u) = \mathbf{r} \text{ and } \sigma(\mathbf{w}) = \sigma(\mathbf{c}) = \mathbf{p}$$

is  $q_{\text{UCQ}}^{\mathcal{K}}$  such that:

$$q_{\text{UCQ}}^{\mathcal{O}}(x) = (R(\mathbf{h}) \wedge \text{ww}(\mathbf{h}, x) \wedge \text{sup}(y, x)) \quad (1)$$

$$\vee (R(\mathbf{h}) \wedge \text{ww}(\mathbf{h}, x) \wedge \text{PhD}(x)) \quad (2)$$

$$\vee (\textcolor{blue}{R(\mathbf{h})} \wedge \textcolor{blue}{\text{sup}(\mathbf{h}, x)}) \quad (3)$$

$$\vee (R(\mathbf{h}) \wedge \text{ww}(x, \mathbf{h}) \wedge \text{sup}(y, x)) \quad (4)$$

$$\vee (R(\mathbf{h}) \wedge \text{ww}(x, \mathbf{h}) \wedge \text{PhD}(x)) \quad (5)$$

$$\vee (R(\mathbf{h}) \wedge \text{sup}(x, \mathbf{h}) \wedge \text{sup}(y, x)) \quad (6)$$

$$\vee (R(\mathbf{h}) \wedge \text{sup}(x, \mathbf{h}) \wedge \text{PhD}(x)) \quad (7)$$

$$q_{\text{UCQ}}^{\mathcal{K}} = \Omega(q_{\text{UCQ}}^{\mathcal{O}}, \mathcal{S}) = (R(\mathbf{h}) \wedge \text{ww}(\mathbf{h}, x) \wedge \text{sup}(y, x)) \quad (1)$$

$$\vee (R(\mathbf{h}) \wedge \text{ww}(\mathbf{h}, x) \wedge \text{PhD}(x)) \quad (2)$$

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# Data-dependent FO-rewriting by example

## Running example (cont.)

The optimization of  $q_{\text{USCQ}}^{\mathcal{O}}$  with

$$\mathcal{S} = \{R(\mathbf{r}), \text{sup}(\mathbf{r}, \mathbf{p}), \text{PhD}(\mathbf{p}), \text{ww}(\mathbf{r}, \mathbf{r}), \text{ww}(\mathbf{r}, \mathbf{p})\}$$

and the database-to-summary homomorphism

$$\sigma(\mathbf{f}) = \sigma(\mathbf{h}) = \sigma(u) = \mathbf{r} \text{ and } \sigma(\mathbf{w}) = \sigma(\mathbf{c}) = \mathbf{p}$$

is  $q_{\text{USCQ}}^{\mathcal{K}}$  such that:

$$q_{\text{USCQ}}^{\mathcal{O}}(x) = (R(\mathbf{h}))$$

$$\wedge (\text{ww}(\mathbf{h}, x) \vee \text{sup}(\mathbf{h}, x) \vee \text{ww}(x, \mathbf{h}) \vee \text{sup}(x, \mathbf{h}))$$

$$\wedge (\text{sup}(y, x) \vee \text{PhD}(x))$$

$$q_{\text{USCQ}}^{\mathcal{K}} = \Omega(q_{\text{USCQ}}^{\mathcal{O}}, \mathcal{S}) = (R(\mathbf{h}))$$

$$\wedge (\text{ww}(\mathbf{h}, x) \vee \text{sup}(\mathbf{h}, x) \vee \text{ww}(x, \mathbf{h}))$$

$$\wedge (\text{sup}(y, x) \vee \text{PhD}(x))$$

# Data-dependent FO-rewriting by example

## Running example (cont.)

The optimization of  $q_{\text{JUCQ}}^{\mathcal{O}}$  with

$$\mathcal{S} = \{R(\mathbf{r}), \text{sup}(\mathbf{r}, \mathbf{p}), \text{PhD}(\mathbf{p}), \text{ww}(\mathbf{r}, \mathbf{r}), \text{ww}(\mathbf{r}, \mathbf{p})\}$$

and the database-to-summary homomorphism

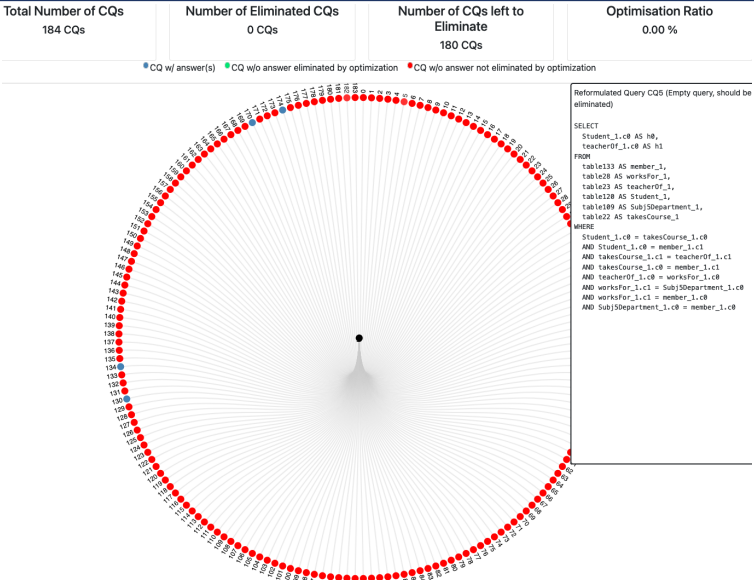
$$\sigma(\mathbf{f}) = \sigma(\mathbf{h}) = \sigma(u) = \mathbf{r} \text{ and } \sigma(\mathbf{w}) = \sigma(\mathbf{c}) = \mathbf{p}$$

is  $q_{\text{JUCQ}}^{\mathcal{K}}$  such that:

$$\begin{aligned} q_{\text{JUCQ}}^{\mathcal{O}}(x) = & (R(\mathbf{h})) \wedge ((\text{ww}(\mathbf{h}, x) \wedge \text{sup}(y, x)) \\ & \vee (\text{ww}(\mathbf{h}, x) \wedge \text{PhD}(x)) \\ & \vee (\text{sup}(\mathbf{h}, x)) \\ & \vee (\text{ww}(x, \mathbf{h}) \wedge \text{sup}(y, x)) \\ & \vee (\text{ww}(x, \mathbf{h}) \wedge \text{PhD}(x)) \\ & \vee (\text{sup}(x, \mathbf{h}) \wedge \text{sup}(y, x)) \\ & \vee (\text{sup}(x, \mathbf{h}) \wedge \text{PhD}(x))) \end{aligned}$$

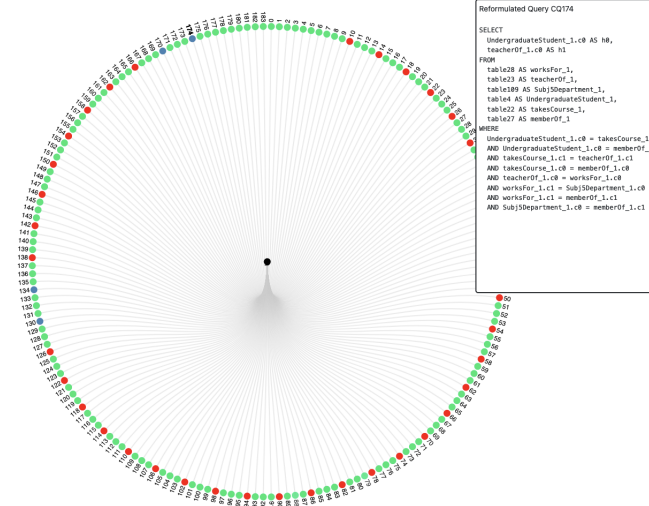
$$q_{\text{JUCQ}}^{\mathcal{K}}(x) = \Omega(q_{\text{JUCQ}}^{\mathcal{O}}, \mathcal{S}) = (R(\mathbf{h})) \wedge ((\text{ww}(\mathbf{h}, x) \wedge \text{sup}(y, x)) \\ \vee (\text{ww}(\mathbf{h}, x) \wedge \text{PhD}(x)) \\ \vee (\text{sup}(\mathbf{h}, x)))$$

# Sample experimental results

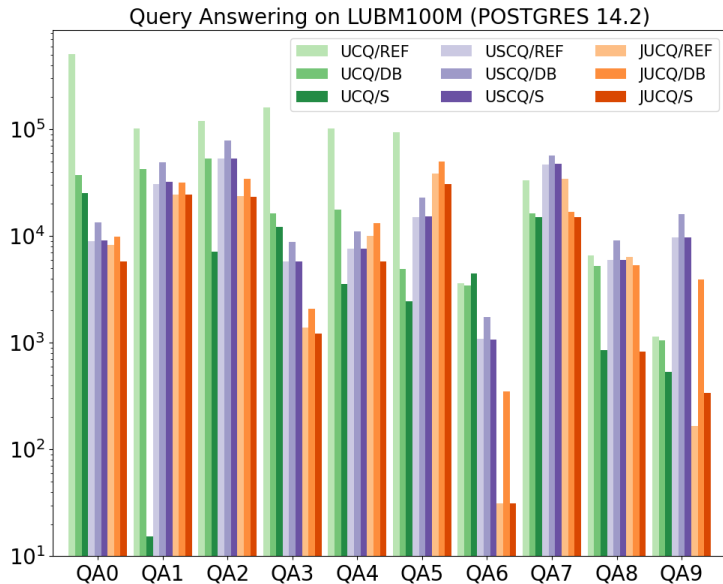


# Sample experimental results

|                                                                                                             |                                     |                                           |                               |
|-------------------------------------------------------------------------------------------------------------|-------------------------------------|-------------------------------------------|-------------------------------|
| Total Number of CQs<br>184 CQs                                                                              | Number of Eliminated CQs<br>142 CQs | Number of CQs left to Eliminate<br>38 CQs | Optimisation Ratio<br>78.89 % |
| ● CQ w/ answer(s) ● CQ w/o answer eliminated by optimization ● CQ w/o answer not eliminated by optimization |                                     |                                           |                               |

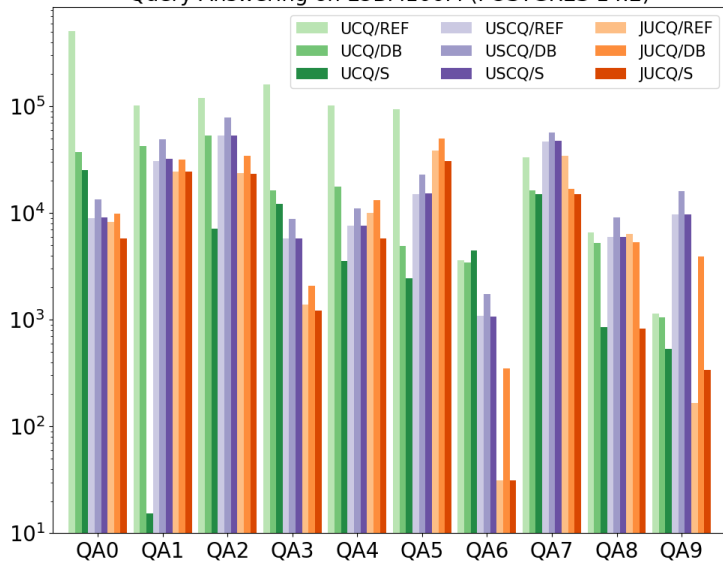


# Sample experimental results



# Sample experimental results

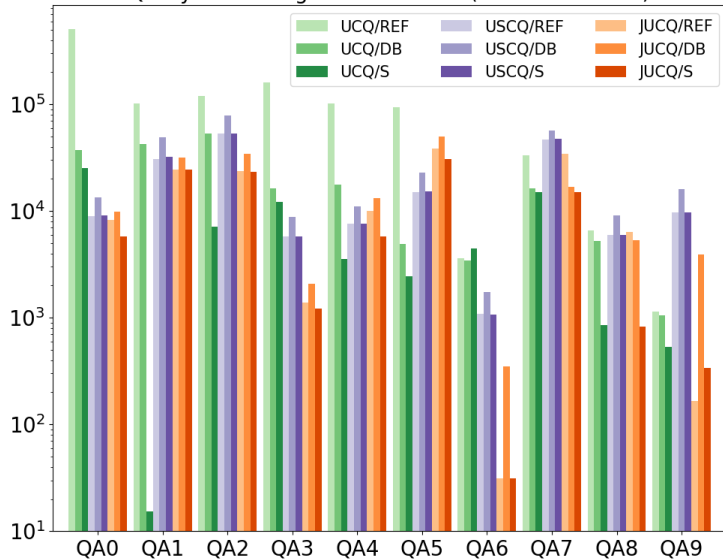
Query Answering on LUBM100M (POSTGRES 14.2)



Optimization scope for  
UCQ/JUCQ/USCQ:

# Sample experimental results

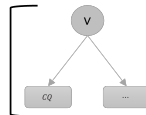
Query Answering on LUBM100M (POSTGRES 14.2)



Optimization scope for

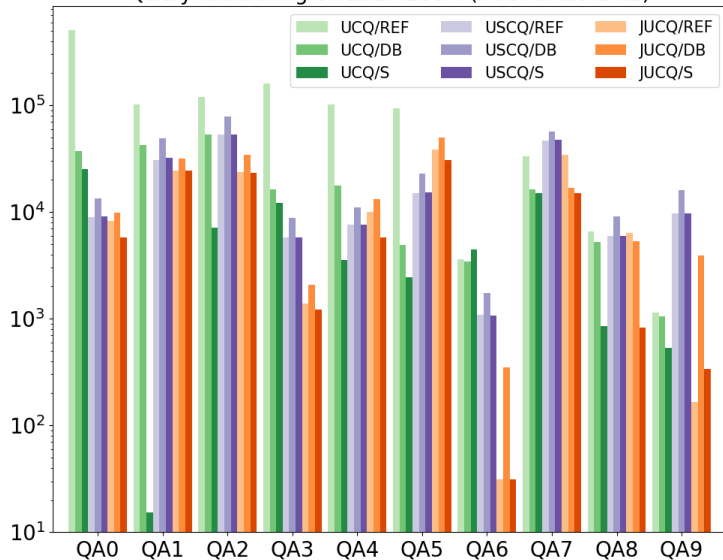
UCQ/JUCQ/USCQ:

$|t|$



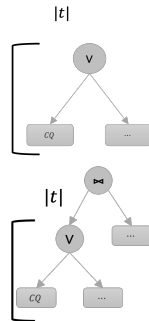
# Sample experimental results

Query Answering on LUBM100M (POSTGRES 14.2)



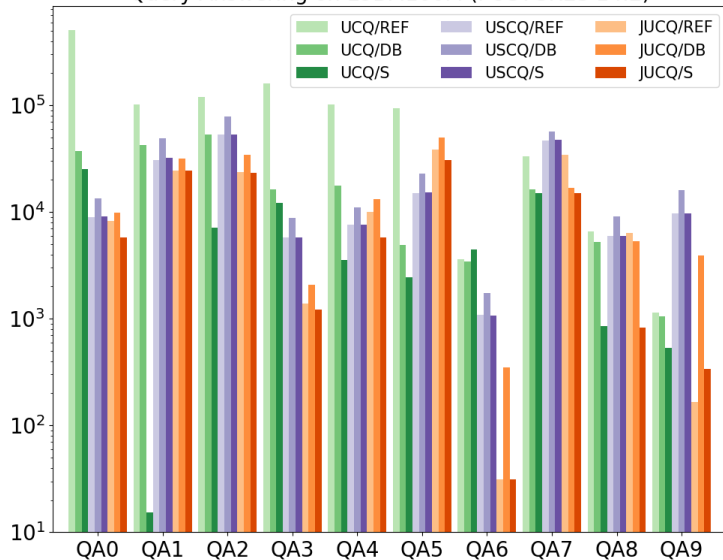
Optimization scope for

UCQ/JUCQ/USCQ:



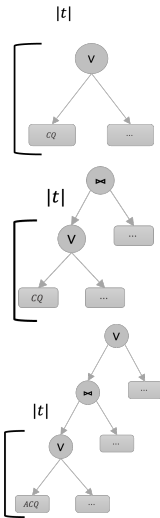
# Sample experimental results

Query Answering on LUBM100M (POSTGRES 14.2)



Optimization scope for

UCQ/JUCQ/USCQ:



## Take home message

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1. FO-rewriting produces **complex rewritings w.r.t. OMQA on a fixed database**
2. OMQA via FO-rewriting can be **optimized for a database with a summary of it**
3. The summary-based optimization OMQA via FO-rewriting **significantly improves performance for UCQ and JUCQ rewritings**

## Related work and contributions

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Some references from the literature on devising OMQA via FO-rewriting for CQs:

| Ontology language                | Query rewriting language                        |                                  |                          |                       |
|----------------------------------|-------------------------------------------------|----------------------------------|--------------------------|-----------------------|
|                                  | UCQ                                             | USCQ                             | JUCQ                     | datalog <sup>nr</sup> |
| datalog $\pm$ /existential rules | [GOP11, GOP14, KLMT15] <a href="#">[HVGJ24]</a> | [Tho13] <a href="#">[HVGJ24]</a> | <a href="#">[HVGJ24]</a> | [OP11, GS12]          |
| description logics/OWL           | [CDL <sup>+</sup> 07, PHM09, CTS11, VSS12]      |                                  | <a href="#">[BGM16]</a>  | [RA10]                |
| RDFS                             | <a href="#">[GMR13, BGMM19]</a>                 |                                  | <a href="#">[BGM15]</a>  |                       |

# Conclusion and perspectives

# Main perspectives

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1. FO-rewriting techniques that produce **directly** rewritings optimized for a database
  - with Maxime Buron (Clermont) and Cheikh-Brahim El Vaigh (Dijon)
2. Data-dependent FO-rewriting in OMQA settings that **are not FO-rewritable**
  - with Maxime Buron & Farouk Toumani (Clermont), Hélène Jaudoin (Rennes), and Quentin Manière & Federico Ulliana (Montpellier)

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